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# Experimental Verification of a Fractional-Order Wien Oscillator Built Using Solid-State Capacitors

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**Abstract**—A new type of fractional-order capacitors (FOCs) is fabricated using a molybdenum disulfide ( $\text{MoS}_2$ )-ferroelectric polymer composite. The phase angle of this FOC's impedance remains constant between 100 Hz and 10 MHz with only a small deviation of  $\pm 4$  degrees. The performance of the fabricated FOCs is further tested using the well-known Wien oscillator. The main motivation of this paper is to demonstrate the use of a broadband, and tunable FOC in a real world application.

**Keywords**—composite materials; constant phase element; fractional-order capacitor; Wien oscillator

## I. INTRODUCTION

Impedance of a fractional-order capacitor (FOC) is expressed as  $Z(s) = s^{-\alpha}(C_\alpha)^{-1}$ , where  $\alpha$  is the fractional order ( $0 < \alpha < 1$ ),  $C_\alpha$  is the pseudo-capacitance (in units of  $\text{F} \cdot \text{s}^{\alpha-1}$ ). Here, the (fractional-order) derivative with respect to time is represented with (complex number)  $s^{-\alpha}$  in the Laplace domain. The fractional order  $\alpha$ , which is an additional degree of freedom, provides an excellent mechanism to describe memory and heredity properties of various materials and processes. Consequently, mathematical models making use of fractional derivatives can account for such effects more rigorously and accurately than their classical integer-order counterparts. The FOCs represent a way of implementing these mathematical models in electronic circuits. Recently, several approaches to fabricating FOCs have been proposed. For example, the FOCs listed in Table 1 are fabricated using polymer composites with different types of fillers. However, either their frequency range of operation (i.e., the frequency range where  $\alpha$  remains constant) is not wide enough or they are not compatible for integration in electronic circuits.

TABLE I. COMPARISON OF DIFFERENT FOCs

Refs	Composite Materials	Bandwidth	Phase Error
[1]	PMMA coating	200 kHz – 1 MHz	$\pm 2^\circ$
[2]	rGO + polymer	50 kHz – 2 MHz	$\pm 3^\circ$
[3]	IPMCs	1 Hz – 10 kHz	Not given
[4, 5]	Poly-based poly. com.	100 kHz – 10 MHz	$\pm 4^\circ$
[6]	MWCNT + polymer	150 kHz – 2 MHz	$\pm 3^\circ$
This work	$\text{MoS}_2$ +polymer	100 Hz – 10 MHz	$\pm 4^\circ$

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In this work, printed circuit board (PCB)-compatible FOCs are fabricated using molybdenum disulfide ( $\text{MoS}_2$ )-ferroelectric polymer composites. These FOCs' frequency range of operation is five decade wide between 100 Hz and 10 MHz. This is broadest constant phase zone that has been reported so far for an FOC. Furthermore, the real-life applicability of these FOCs is demonstrated by using them to design and fabricate a Wien oscillator.

## II. FABRICATION OF FOCs USING $\text{MoS}_2$ -POLYMER COMPOSITES

### A. Fabrication Procedure

The fabricated FOC is shown in Fig. 1(a). The bottom electrode is 200 nm Au sputtered on  $\text{SiO}_2/\text{Si}$  substrate while the top electrode is sputtered on the dielectric composite with same thickness / material using a circular electrode with 3 mm diameter shadow mask where nine individual FOCs are fabricated on a  $2 \text{ cm} \times 2 \text{ cm}$  sample area. The mixture of 0.03 g/ml  $\text{MoS}_2$  and 0.1 g/ml polymer (PVDF-TrFE-CFE) in N, N-Dimethylformamide (DMF) solvent drop-casted onto the bottom electrode. The sample is flip-bonded on a PCB, so that each capacitor provides a separate connection for electrical measurements.

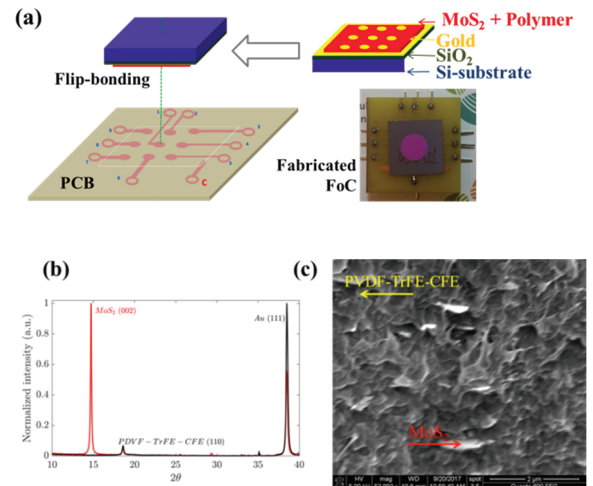


Fig. 1. (a) PCB compatible FOC fabricated using  $\text{MoS}_2$ -polymer composite. (b) XRD spectra for PVDF-TrFE-CFE and  $\text{MoS}_2$  / PVDF-TrFE-CFE. (c) Its cross-sectional SEM image.

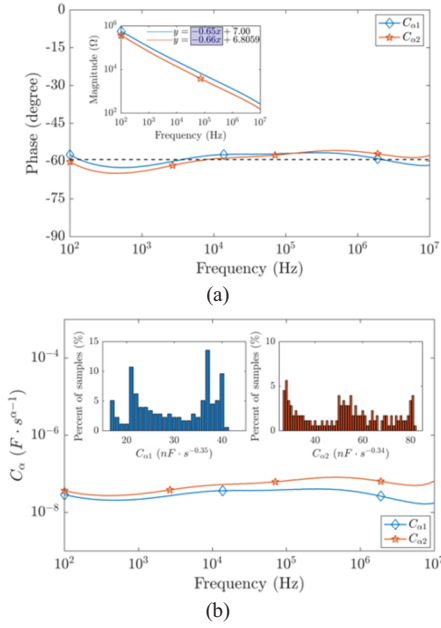


Fig. 2. (a) Phase and magnitude of the impedance and (b) pseudocapacitance of the fabricated FOCs.

### B. Imaging and Characterization of the FOCs

X-ray powder diffraction (XRD) patterns of the pristine polymer, PVDF-TrFE-CFE and MoS<sub>2</sub> composite, are shown in Fig. 1(b). We observe intense peak at 14.77° which belongs to MoS<sub>2</sub>. These results also show that no additional complex molecular structures are formed in the composite. Furthermore, the scanning electron microscopy (SEM) image provided in Fig. 1(c) shows that the MoS<sub>2</sub> nanosheets are homogeneously distributed inside the composite. The impedance of two fabricated FOCs is analyzed using the Agilent 4994A Precision Impedance Analyzer with the 16048G model test fixture. Fig. 2(a) plots the phase of the impedance versus frequency and shows that it remains constant at -58.5° and -59.4° with only ±4° phase deviation between 100 Hz and 10 MHz (five decades) for both of the FOCs. The pseudocapacitances of these FOCs, which are extracted from impedance magnitude measurements, are shown in Fig. 2(b). Their values at 25 kHz are  $C_{01} = 37.2 \text{ nF} \cdot \text{s}^{-0.35}$  and  $C_{02} = 55.2 \text{ nF} \cdot \text{s}^{-0.34}$ . It should be noted here the constant phase angle can be tuned by using different types of polymers in the composite.

### III. FRACTIONAL-ORDER WIEN OSCILLATOR

The performance of the fabricated FOCs is demonstrated by using them to fabricate a fractional-order Wien oscillator (Fig. 3). In the circuit in Fig. 3,  $R_1 = R_2 = 10 \text{ k}\Omega$ ,  $R_3 = 47 \text{ k}\Omega$ ,  $C_{01} = 37.2 \text{ nF} \cdot \text{s}^{-0.35}$ , and  $C_{02} = 55.2 \text{ nF} \cdot \text{s}^{-0.34}$ . The measured frequency of oscillation (FO) is 24.87 kHz while the one calculated using the above values is 23.52 kHz [7]. The measurement is repeated after the FOCs are replaced with two conventional capacitors with a capacitance value of 30 nF and 50 nF. For this case the FO is measured to be 0.414 kHz. This demonstrates that the fractional-order Wien oscillator has a significantly higher FO that its conventional counterpart. It should also be noted here that the peak-to-peak amplitudes of the output voltage of both oscillators are same and equal to 1.88 V.

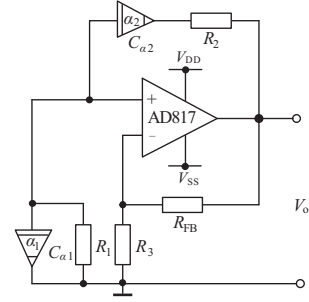


Fig. 3. Schematic of fractional-order Wien oscillator.

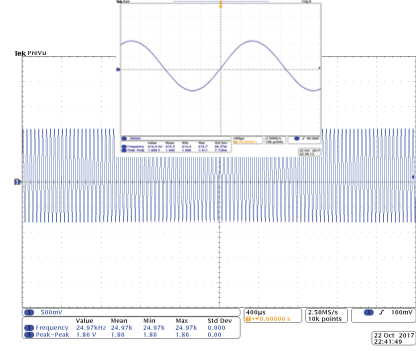


Fig. 4. Measured steady-state output voltage waveform of the fractional-order Wien oscillator and the conventional one as an inset.

### IV. CONCLUSION

A tunable FOC with a frequency range of operation changing from 100 Hz to 10 MHz (five decades) is introduced. The phase angle of the FOC's impedance varies within only ±4° in this frequency range. The performance of the FOCs is demonstrated by using them to design and fabricate a fractional-order Wien oscillator.

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